CS 61A Spring 2025

Structure and Interpretation of Computer Programs

MIDTERM 1 SOLUTIONS

INSTRUCTIONS

This is your exam. Complete it either at exam.cs61a.org or, if that doesn't work, by emailing course staff with your solutions before the exam deadline.

This exam is intended for the student with email address <EMAILADDRESS>. If this is not your email address, notify course staff immediately, as each exam is different. Do not distribute this exam PDF even after the exam ends, as some students may be taking the exam in a different time zone.

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For questions with circular bubbles, you should select exactly one choice.
○ You must choose either this option
Or this one, but not both!
For questions with square checkboxes , you may select <i>multiple</i> choices.
☐ You could select this choice.
☐ You could select this one too!
You may start your exam now. Your exam is due at <deadline> Pacific Time. Go to the next page to begin.</deadline>

Preliminaries

(a)	What is your full name?
(b)	What is your student ID number?

You can complete and submit these questions before the exam starts.

(c)	What is your @berkeley.edu email address?

` '	Sign (or type) your name to confirm that all work on this exam will be your own. The penalty misconduct on an exam is an F in the course.	for academic

1. (6.0 points) What Would Python Print?

```
Answer the questions about this code. No errors occur while it is executed.
```

```
def double(x):
    return 2 * x

def square(f):
    return lambda x: f(x) * f(x)

def inc(f):
    return lambda x: f(x + 1)

def triple(f):
    return lambda x: f(f(f(x)))

def put(x):
    return lambda f: f(x)
```

(a) (2.0 pt) What is displayed by the last line?

```
5
None
None
```

(b) (2.0 pt) What would be displayed by evaluating print(one(square(double)))

```
4
```

(c) (2.0 pt) What would be displayed by evaluating print(inc(put)(1)(triple(double)))

```
16
```

(d) (0.0 pt) This A+ question is not worth any points. It can only affect your course grade if you have a high A and might receive an A+. Finish the rest of the exam first!

Write one line of code just after triple(print)(5) that would double and add one to all numbers in the answers to parts (b) and (c) above. For example, for an answer containing 100, it would now contain 201 instead.

You may not use any numbers or arithmetic symbols (such as + or *) or arithmetic functions (such as add or mul). You may not reassign triple or square. You may use multiple assignment: x, $y = _{--}$, $_{--}$

```
Four possible answers:

print = (lambda f: lambda x: f(double(x)))(inc(print))

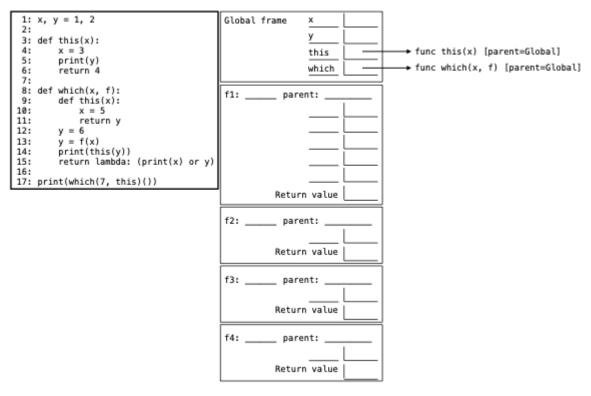
print = (lambda f: lambda x: inc(f)(double(x)))(print)

f, print = inc(print), lambda x: f(double(x))

f, print = print, lambda x: inc(f)(double(x))
```

2. (8.0 points) Which One

Complete the environment diagram below to answer the questions about the calls to print. Only the questions will be scored, not the diagram. Each call to print is evaluated once, and there are no errors caused by running this code.



(a) (2.0 pt) What is displayed by the call to print on line 5?

2

(b) (2.0 pt) What is displayed by the call to print on line 14?

4

(c) (2.0 pt) What is displayed by the call to print on line 15?

7

(d) (2.0 pt) What is displayed by the call to print on line 17?

4

3. (13.0 points) Legit Digit

odd(n)
 cond(n)

(a) (4.0 points)

Implement all_digits, which takes a positive integer n and one-argument function cond that always returns True or False. It returns True if cond(d) returns True when called on every digit d in n, and False otherwise.

```
def all_digits(n, cond):
    """Return whether cond returns true for every digit of positive n.
    >> odd = lambda d: d % 2 == 1
    >>> all_digits(123, odd) # not all digits are odd
    False
    >>> all_digits(357, odd) # all digits are odd
    True
    while n:
        if ____:
             (a)
               (b)
        n = n // 10
    return _____
             (c)
 i. (2.0 pt) Fill in blank (a).
      not cond(n % 10)
ii. (1.0 pt) Fill in blank (b).
   \bigcirc n = n % 10
   \bigcirc n = n * 10
   O return True
    return False
   O return odd
   O return cond
iii. (1.0 pt) Fill in blank (c).
   \bigcirc n
    True
   ○ False
```

(b) (3.0 points)

Definition. A prefix of a positive integer n is the value of n//pow(10, p) for some non-negative integer p. For example, 3456 has prefixes 3456, 345, 34, 3, and 0.

Implement prefix_digits, which takes a positive integer n and a one-argument function cond that always returns True or False. It returns the largest prefix of n for which cond returns True when called on every digit of the prefix. You may call all_digits and process.

```
def process(n, check):
    """A function to help implement prefix_digits."""
   while n:
        if check(n):
           return n
       n = n // 10
   return 0
def prefix_digits(n, cond):
    """Return the largest prefix of positive n for which cond returns true for every digit.
   >>> odd = lambda d: d % 2 == 1
   >>> prefix_digits(94720, odd)
   >>> prefix_digits(919321, odd)
   9193
   >>> prefix_digits(2025, odd)
   >>> prefix_digits(20252025, lambda d: d < 4)
   >>> prefix_digits(20252025, lambda d: True)
    20252025
   return process(n, lambda k: _____)
 i. (3.0 pt) Fill in blank (d).
   all_digits(n, cond)
   all_digits(k, cond)
   all_digits(n, cond(n))
   all_digits(k, cond(k))
   lambda cond: all_digits(n, cond)
   lambda cond: all_digits(k, cond)
   lambda cond: all_digits(n, cond(n))
   lambda cond: all_digits(k, cond(k))
   all_digits(n, lambda n: cond)
    all_digits(k, lambda n: cond)
    all_digits(n, cond(lambda n: n))
```

all_digits(k, cond(lambda n: k))

(c) (6.0 points)

Re-implement prefix_digits, which takes a positive integer n and a one-argument function cond that always returns True or False. It returns the largest prefix of n for which cond returns True when called on every digit of the prefix. You may not call all_digits or process.

```
def prefix_digits(n, cond):
    """Return the largest prefix of positive n for which cond returns true for every digit.
    >>> odd = lambda d: d % 2 == 1
    >>> prefix_digits(94720, odd)
    >>> prefix_digits(919321, odd)
    9193
    >>> prefix_digits(2025, odd)
    >>> prefix_digits(20252025, lambda d: d < 4)
    202
    11 11 11
    k = 0
    while n >= ____:
                  (e)
        if cond(_____):
                   (f)
            k += 1
        else:
            n = n // 10
              (g)
    return n
 i. (2.0 pt) Fill in blank (e).
   \bigcirc 0
   () k
   O k // 10
   pow(10, k)
ii. (2.0 pt) Fill in blank (f).
   O n % 10
   O n // 10 % 10
   O n % pow(10, k)
   \bigcirc n // pow(10, k)
   O n // 10 % pow(10, k)
   on // pow(10, k) % 10
```

iii. (2.0 pt) Fill in blank (g). You may not call all_digits or process.

```
\mathbf{k}=\mathbf{0}
```

4. (4.0 points) Hailstone Returns

Definition. A hailstone sequence is formed by picking a positive integer n as the start then repeatedly updating n until it is 1 using this rule: if n is even, divide it by 2; if n is odd, multiply it by 3 and add 1.

Implement hailstone, which prints each update in a hailstone sequence by displaying: the update number (counting up from 1), the current n, an -> arrow symbol, and the updated n.

This implementation may not be possible using the template. If that's the case, respond *Impossible* to the following questions.

```
def hailstone(n):
```

"""Print numbered updates in the hailstone sequence.

```
>>> hailstone(10)
   1 10 -> 5
   2 5 -> 16
   3 16 -> 8
   4 8 -> 4
   5 4 -> 2
   6 2 -> 1
   11 11 11
   def f():
       if n % 2 == 1:
           m = 3 * n + 1
       else:
           m = n // 2
         (a)
        ____
          (b)
   k = 1
   while n > 1:
       k, n = k + 1, f()
(a) (2.0 pt) Fill in blank (a).
    print(k, n, ->, m)
   print(k, n, '->', m)
   print(k - 1, n, ->, m)
   O print(k - 1, n, '->', m)
   ○ Impossible
```

(b) (2.0 pt) Fill in blank (b). If the problem is not possible using the template, write Impossible.

```
return m
```

5. (4.0 points) It Takes Two

Implement at_least_two, which takes three arguments. It returns True if at least two of them are true values and False otherwise. The built-in bool function takes one argument and returns True if it is a true value and False if it is a false value.

```
def at_least_two(x, y, z):
    """Returns whether at least two of the arguments are true values.
    >>> at_least_two(1 + 1, 3 + 3, 5 + 5)
    True
    >>> at_least_two(1 + 1, 3 - 3, 5 + 5)
    True
    >>> at_least_two(1 - 1, 3 + 3, 5 + 5)
    True
    >>> at_least_two(1 - 1, 3 + 3, 0)
    False
    >>> at_least_two(1 - 1, 0, 0)
    False
    11 11 11
    if ____:
         (a)
        return _____
                  (b)
    else:
        return _____
                  (c)
(a) (2.0 pt) Fill in blank (a).
    O x == True
    O x and y
    x == True and y == True
(b) (1.0 pt) Fill in blank (b). Select all correct answers.
    □ y or z
    \square y and z
    bool(y or z)
    \square bool(y and z)
    \square not(y or z)
    \square not(y and z)
(c) (1.0 pt) Fill in blank (c). Select all correct answers.
    □ y or z
    \square y and z
    ☐ bool(y or z)
    bool(y and z)
    \square not(y or z)
    \square not(y and z)
```

No more questions.